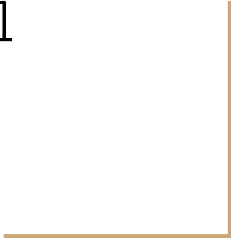


Programming, Problem Solving, and Algorithms

CPSC203, 2019 W1



Announcements

Project 3 released soon. Due 11:59p, Nov 29.

“Problem of the Day” continues!

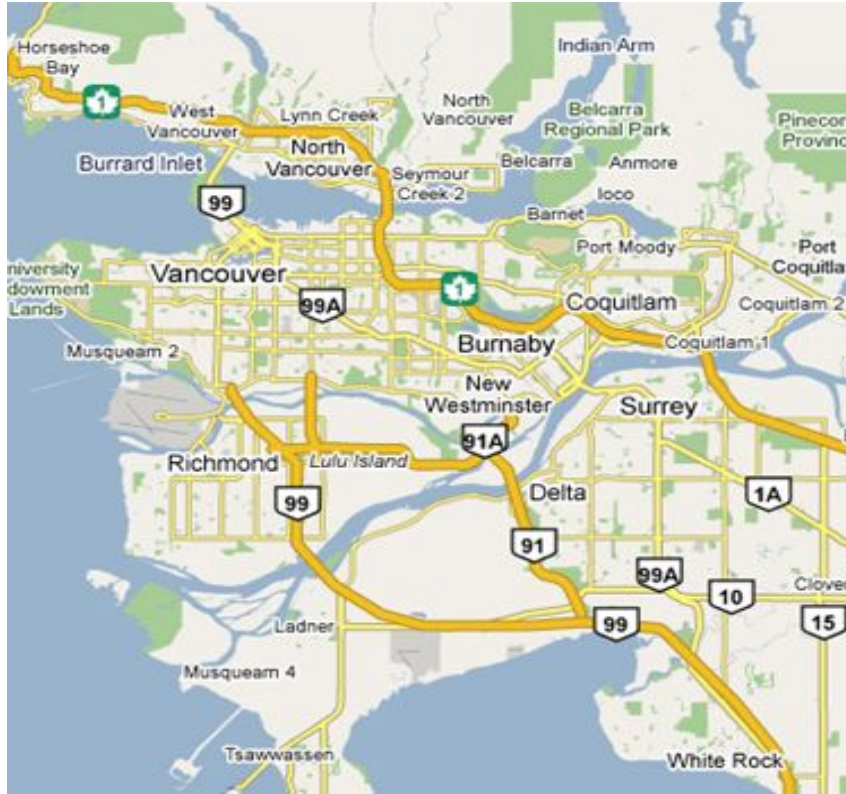
Today:

Shortest Path

Maps!

How many Starbucks are in Vancouver?

Single Source Shortest Path

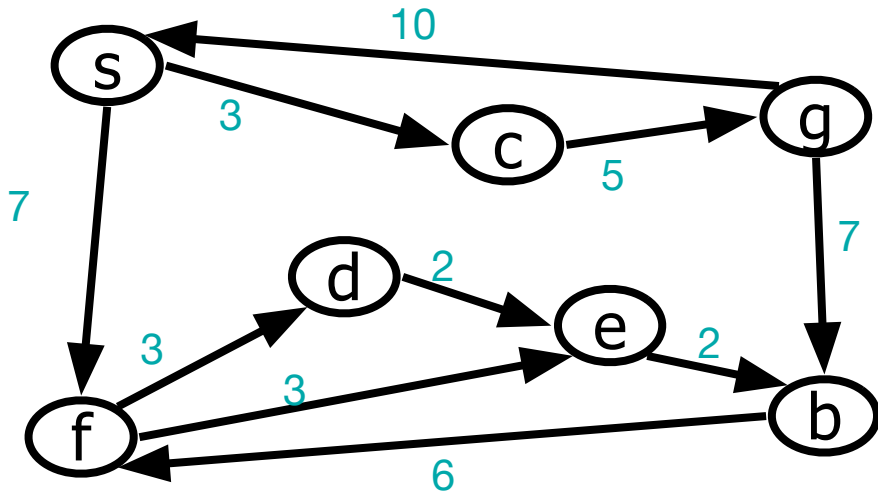


Given a start vertex (source) s , find the path of least total cost from s to every vertex in the graph.

Single Source Shortest Path

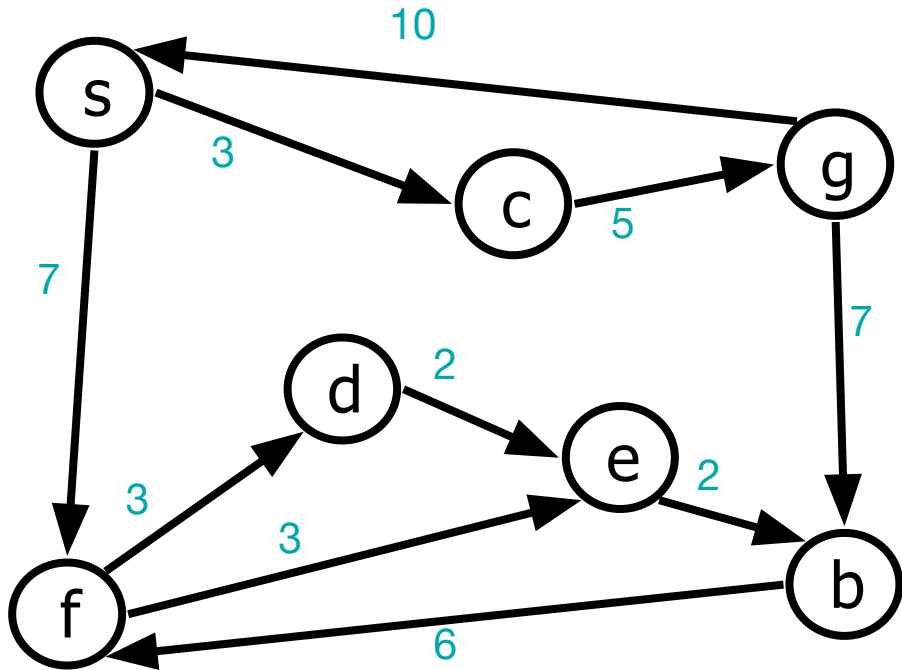
Input: directed graph G with non-negative edge weights, and a start vertex s .

Output: A subgraph G' consisting of the shortest (minimum total cost) paths from s to every other vertex in the graph.



Dijkstra's Algorithm (1959)

Single Source Shortest Path



Given a source vertex s , we wish to find the shortest path from s to every other vertex in the graph.

Initialize structure:

Repeat these steps:

1. Label a new (unlabelled) vertex v , whose shortest distance has been found
2. Update v 's neighbors with an improved distance

Single Source Shortest Path

Initialize structure:

1. For all v , $d[v] = \text{“infinity”}$, $p[v] = \text{null}$
2. Initialize source: $d[s] = 0$
3. Initialize priority (min) queue

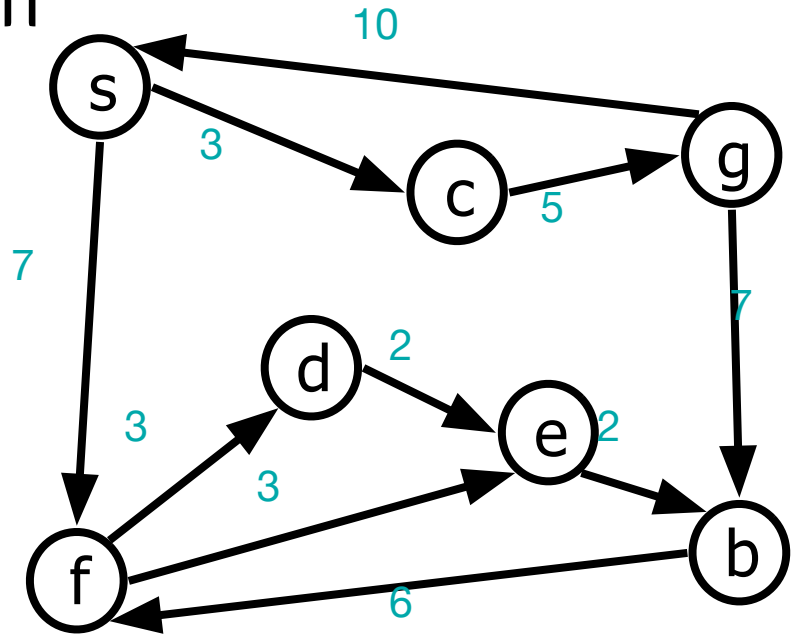
Repeat these steps n times:

- Find minimum $d[]$ unlabelled vertex: v
- Label vertex v
- For all unlabelled neighbors w of v ,

If (_____ $< d[w]$)

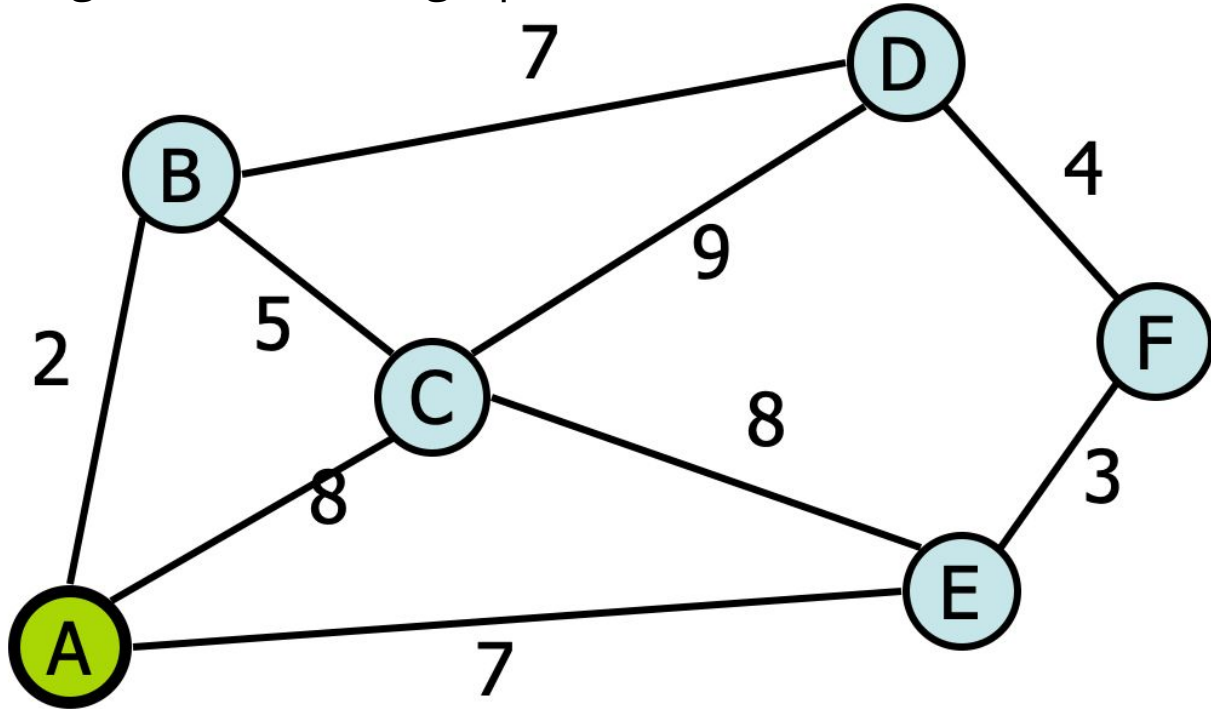
$d[w] =$ _____

$p[w] = v$



Your Turn...

Execute the algorithm on this graph:



Dijkstra's Algorithm

How is this algorithm similar to BFS/DFS?

How is this algorithm different from BFS/DFS?

Initialize structure:

1. For all v , $d[v] = \text{"infinity"}$, $p[v] = \text{null}$
2. Initialize source: $d[s] = 0$
3. Initialize priority (min) queue
4. Initialize set of labeled vertices to \emptyset .

Repeat these steps n times:

- Find & remove minimum $d[]$ unlabelled vertex: v
- Label vertex v
- For all unlabelled neighbors w of v ,
If $\text{cost}(v,w) < d[w]$
 $d[w] = \text{cost}(v,w)$
 $p[w] = v$

Map applications

Three parts:

1. Assembling the data - OSM, local data stores, statsCan, etc. This is mostly the art of assembling geodataframes.
2. Computing on the data - osmnx simplifies graph algorithms and computation, but also supports other spatial computation.
3. Visualizing the data - matplotlib for static maps, folium for interactive maps.

POTD #36 Thu

<https://github.students.cs.ubc.ca/cpsc203-2019w-t1/potd36>

Describe any snags you run into:

1. Line ___: _____
2. Line ___: _____
3. Line ___: _____
4. Line ___: _____
5. Line ___: _____

ToDo for next class...

POTD: Continue every weekday! Submit to repo.

Reading: TLACS Ch 10 & 12 (lists and dictionaries)

References:

<https://www.youtube.com/watch?v=wsSEKm-rU6U>

<https://github.com/gboeing/osmnx-examples/tree/master/notebooks>

<https://gist.github.com/psychemedia/b49c49da365666ba9199d2e27d002d07>